

## Einstein

$E_{ij}$ : symmetric 2-tensor,  
divergence-free

$E = \text{Poly}(g, \partial g, \partial^2 g)$ , linear in  $\partial^2 g$

Critical for  $\int \text{scal}_g \text{ dvol}_g$

Solution space spanned by  $g, \text{Ric}(g)$

DeTurck trick

## Lovelock (generalized Einstein)

$F_{ij}$ : symmetric 2-tensor,  
divergence-free

$F = \text{Poly}(g, \partial g, \partial^2 g)$ , **nonlinear** in  $\partial^2 g$   
allowed

[Lab08]: Critical for  $\int \text{scal}_g^{(2q)} \text{ dvol}_g$

Solution space spanned by  $g, \text{Ric}(g), \text{Ric}^{(4)}(g), \dots, \text{Ric}^{(\lfloor n/2 \rfloor)}(g)$

[Alb20]: DeTurck trick